

# Iterative Closest Point Differencing

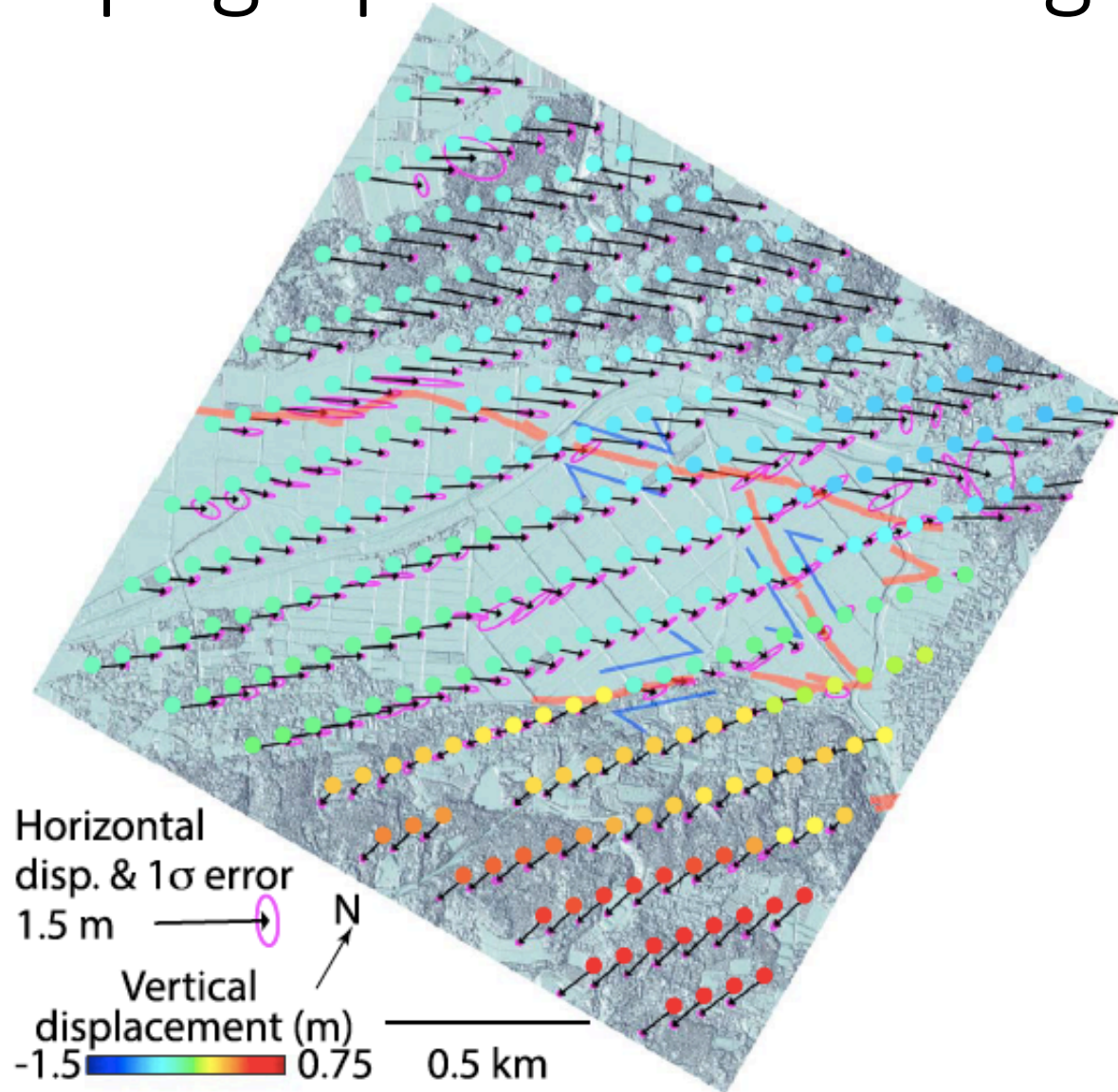
Chelsea Scott

With contributions from Edwin Nissen

# Outline

- Brief motivation
- Technical introduction to differencing
- Processing Choices
  - Window size
  - Grid spacing
  - Coordinate system origin
  - Point-to-point vs. Point-to-plane error penalty
- Matlab demo
- How do I perform topographic differencing on my own datasets?
- PLEASE ASK QUESTIONS!!

# Topographic differencing



- Calculate 3D on- and off-fault deformation
- Resolves deformation along the fault where other geodetic datasets commonly lack resolution
- Method assumes a rigid deformation. Other methods (e.g., PIV) work better when assumption is invalid.

# Iterative Closest Point

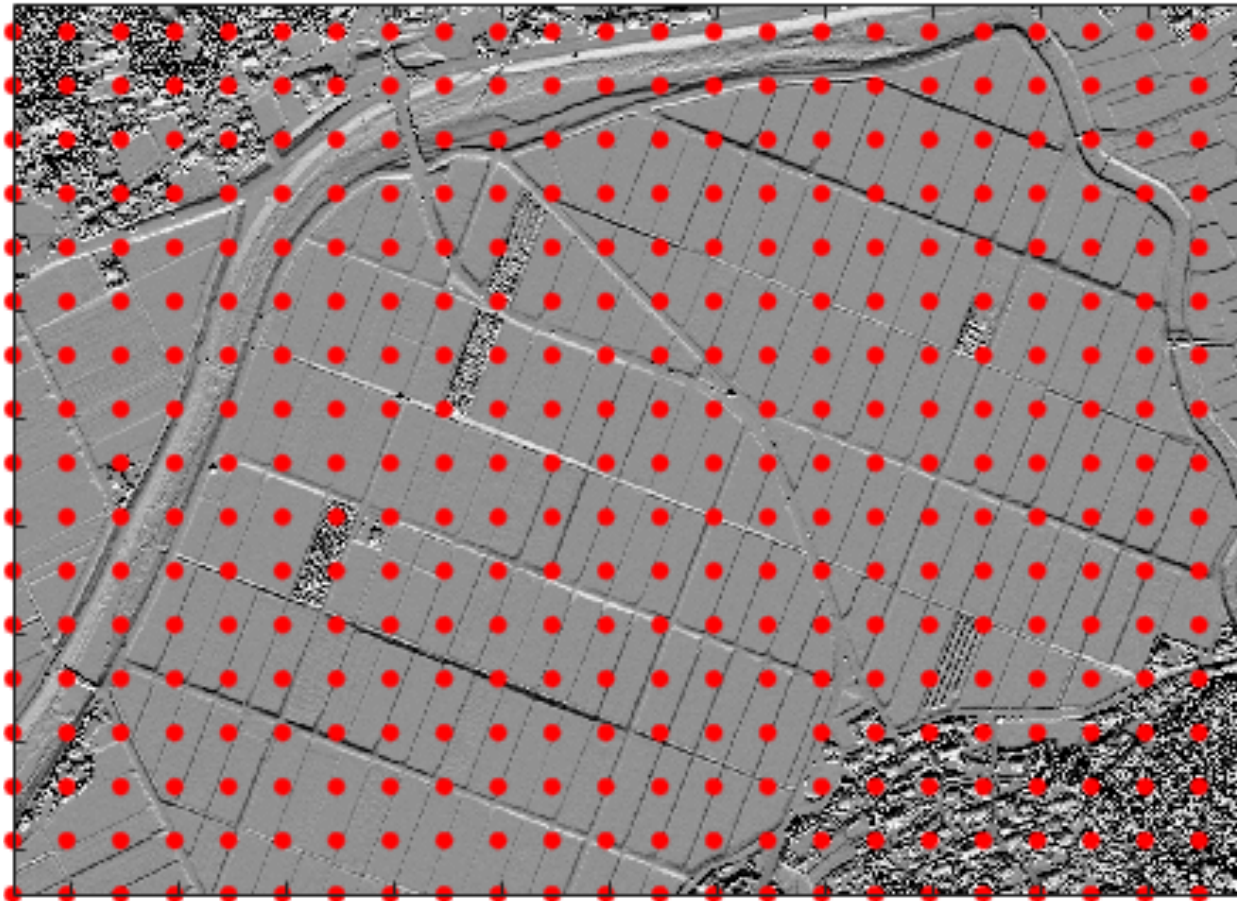


Pre-earthquake: Compare

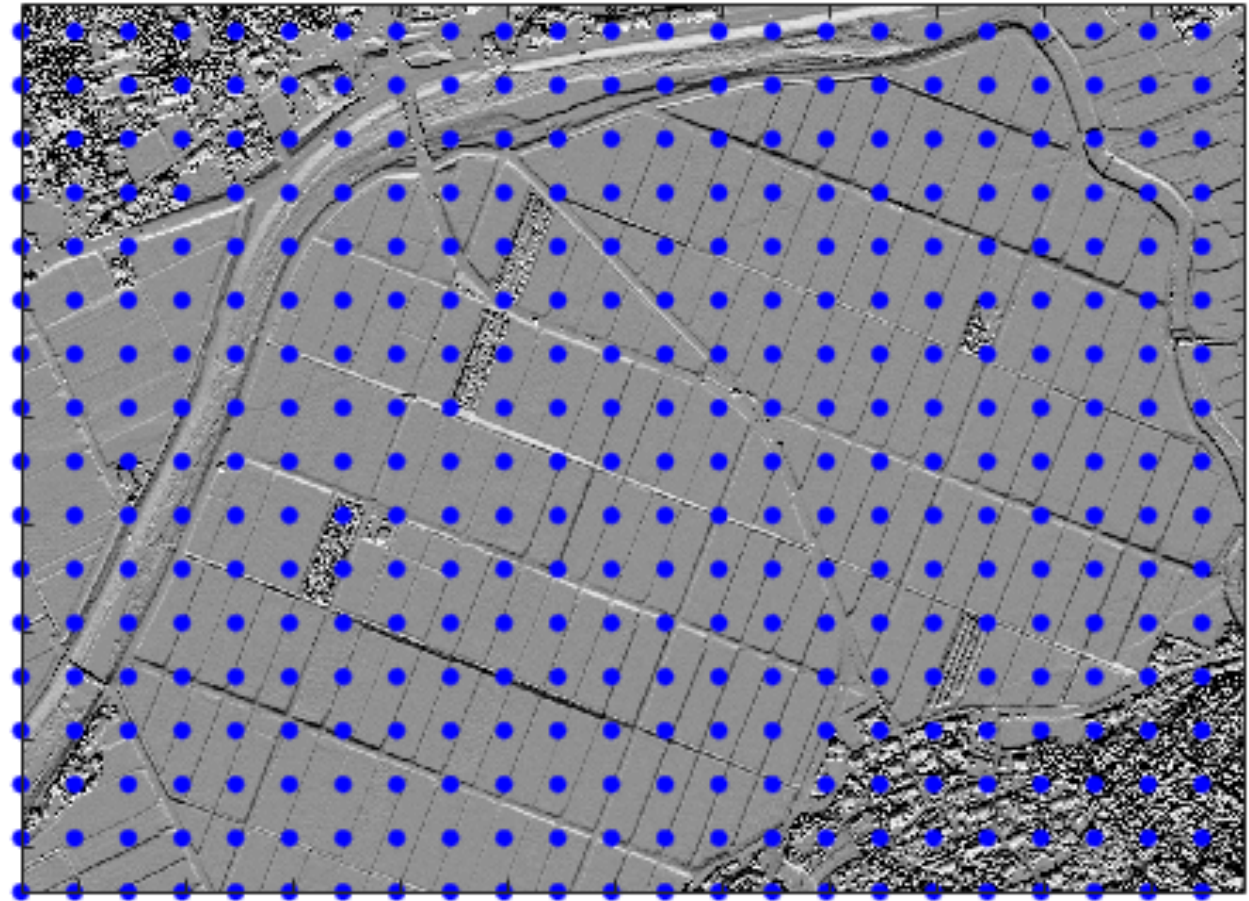


Post-earthquake: Reference

# Calculate 3D displacements at core points

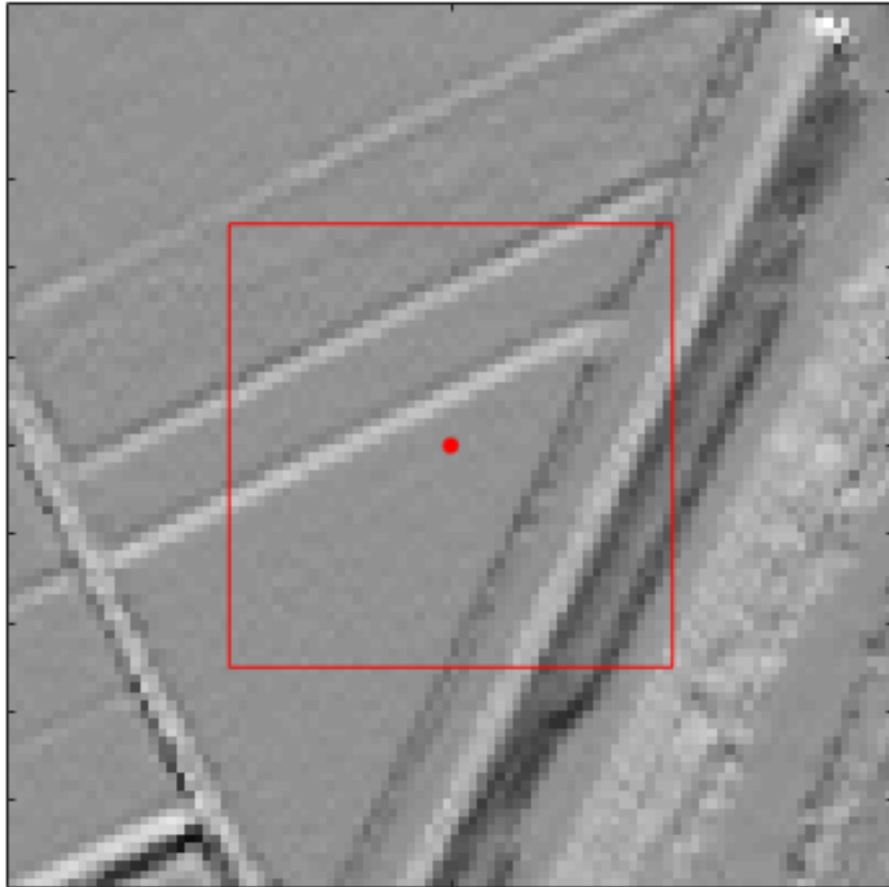


Pre-earthquake: Compare

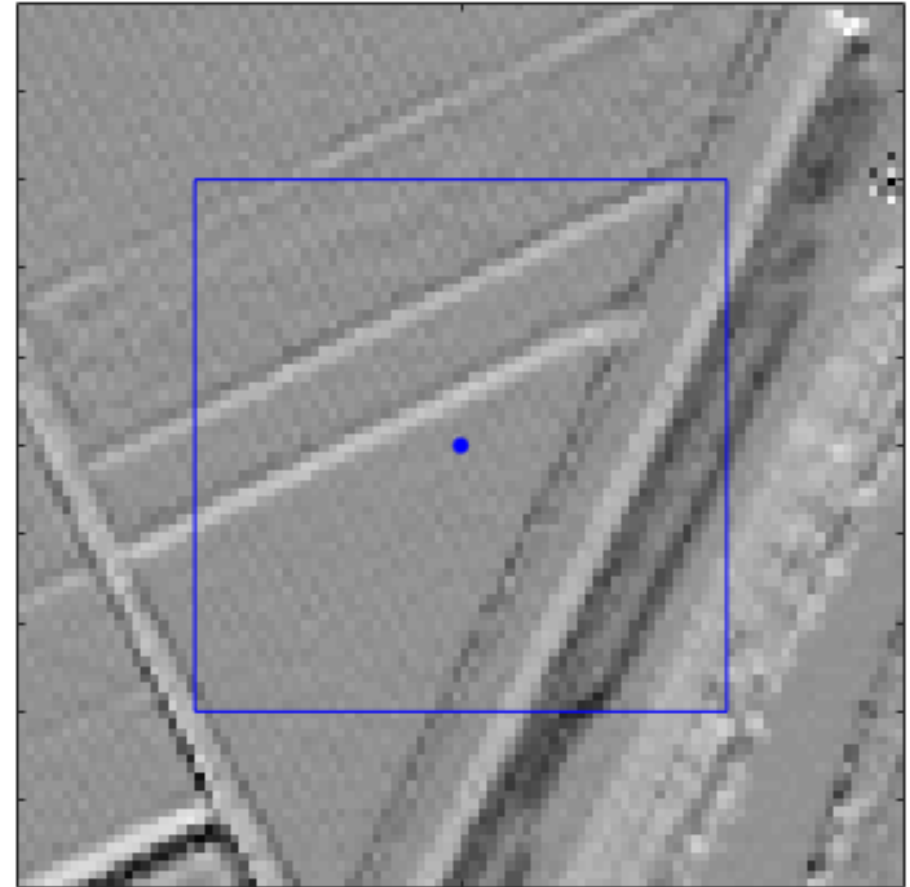


Post-earthquake: Reference

# Select windowed subsets

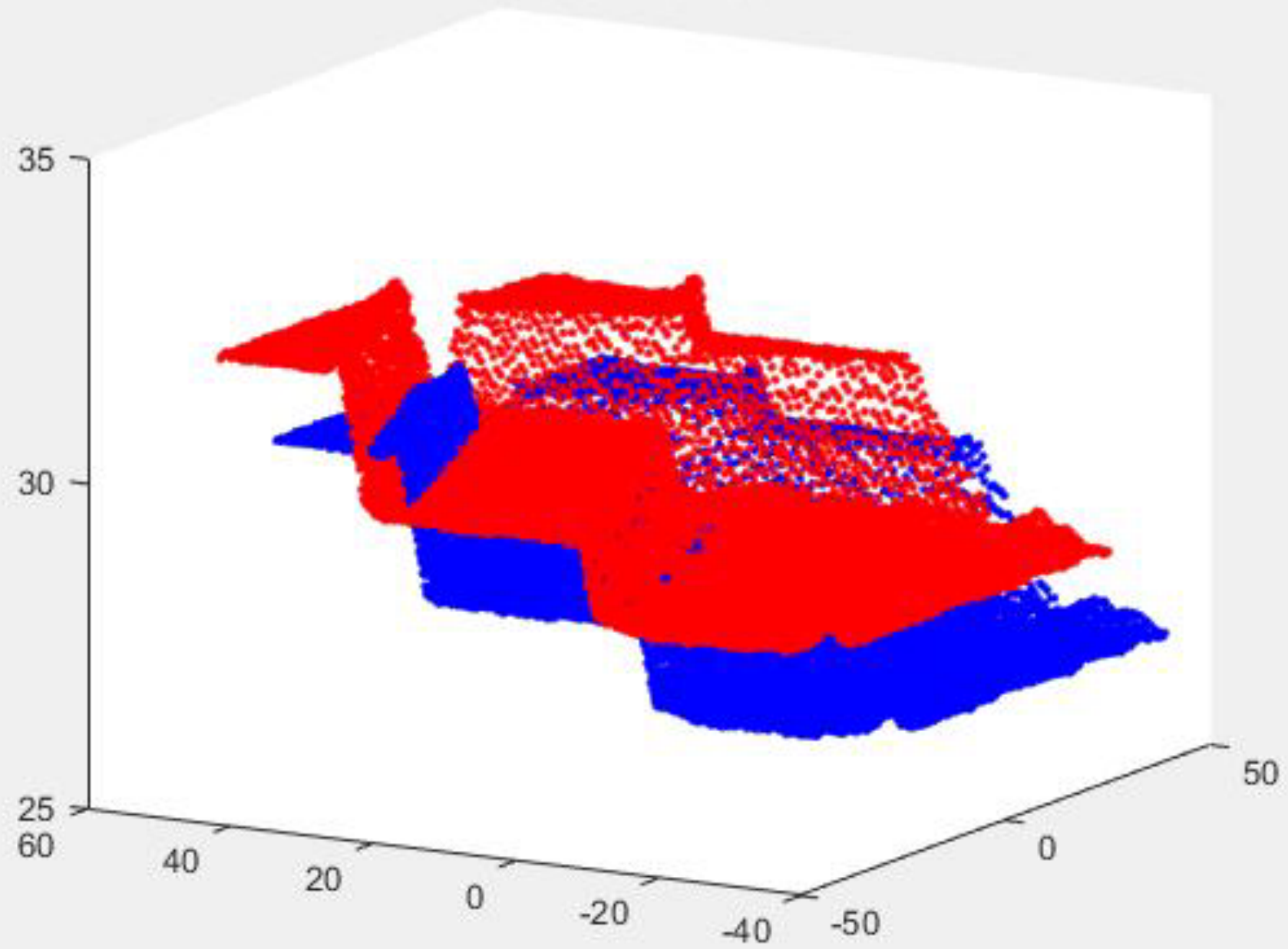


Pre-earthquake: Compare  
Width 50 m



Post-earthquake: Reference  
Contains an extra 10 m buffer

Iteration number: 1

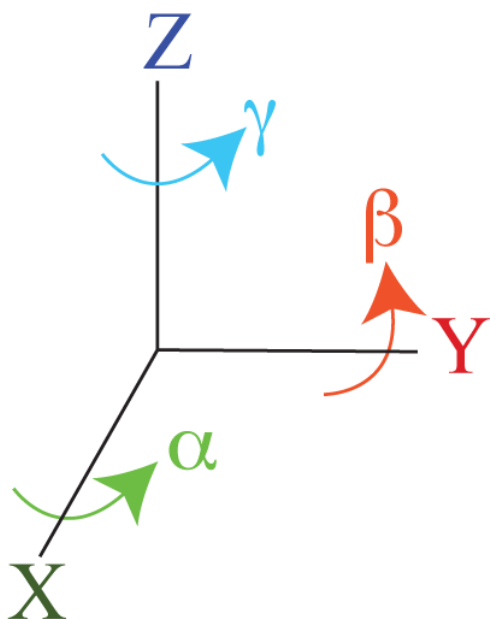


# 3D rigid deformation

Deformed point cloud

$$= \begin{bmatrix} 1 & -\gamma & \beta \\ \gamma & 1 & -\alpha \\ -\beta & \alpha & 1 \end{bmatrix} \begin{bmatrix} \text{Undeformed} \\ \text{point cloud} \end{bmatrix} + \begin{bmatrix} t_x \\ t_y \\ t_z \end{bmatrix}$$

Rotation Translation



Coordinate system

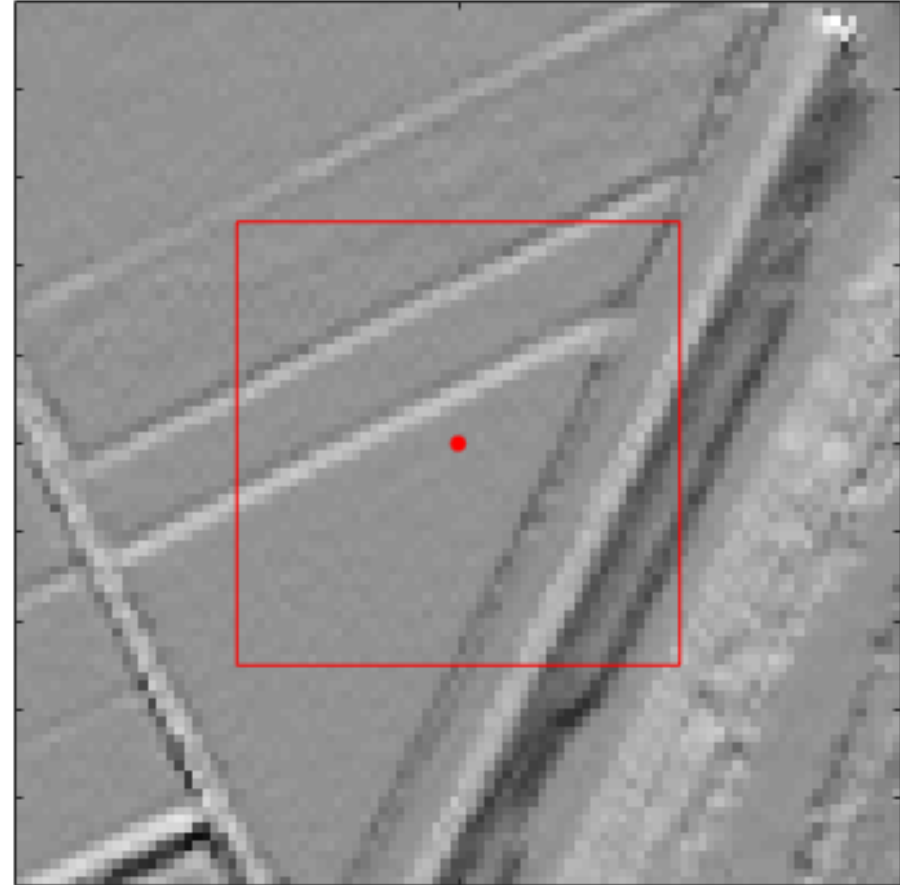


# Processing Choices

- Window Size
- Grid Spacing
- Coordinate system origin
- Point-to-point vs. Point-to-plane error penalty

# Window Size

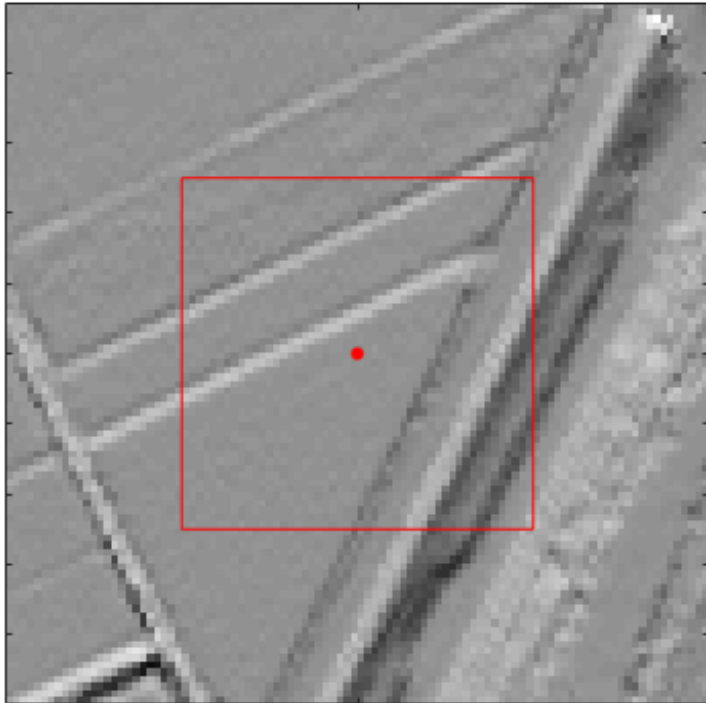
- Large enough that there is sufficient topographic relief to produce an accurate alignment
- Smaller windows have better resolution and a lower violation of the rigid body assumption
- In my experience, 30-50 m window size are best with 1-4 shots/m<sup>2</sup> lidar imagery



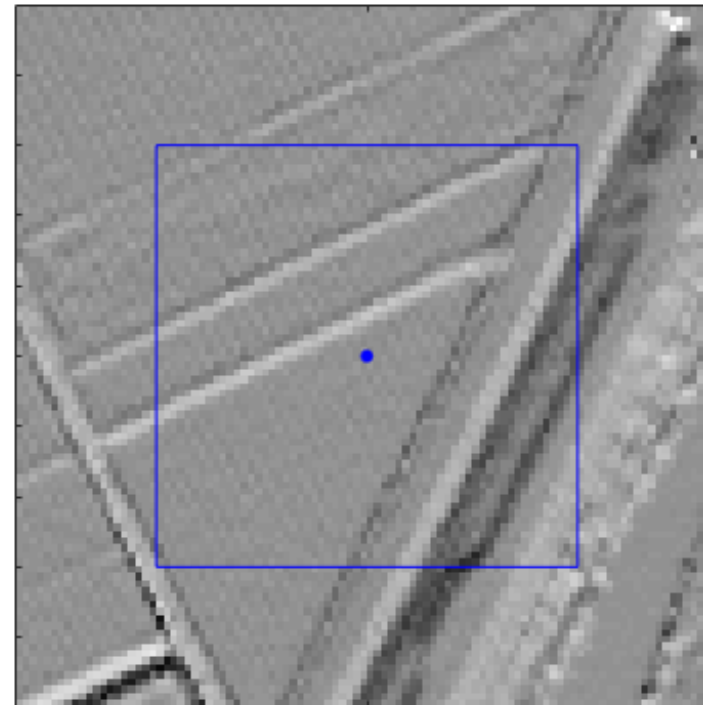
Canal and field boundaries provide topographic relief

# Window size of reference dataset

Add buffer to the reference point cloud so that the deformed reference point cloud fits entirely into the compare point cloud.



Pre-earthquake: Compare  
Width 50 m

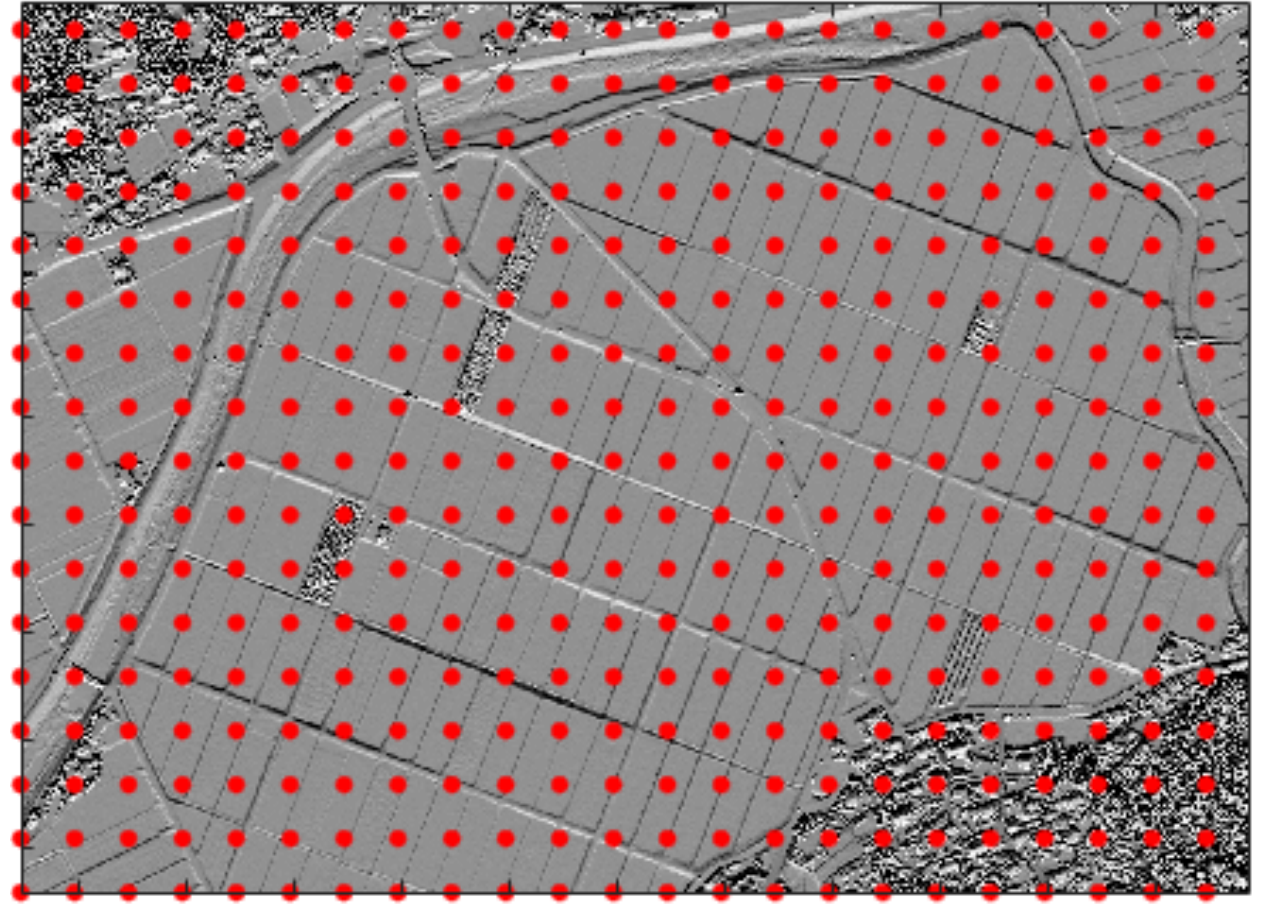


Post-earthquake: Reference  
Contains an extra 10 m buffer

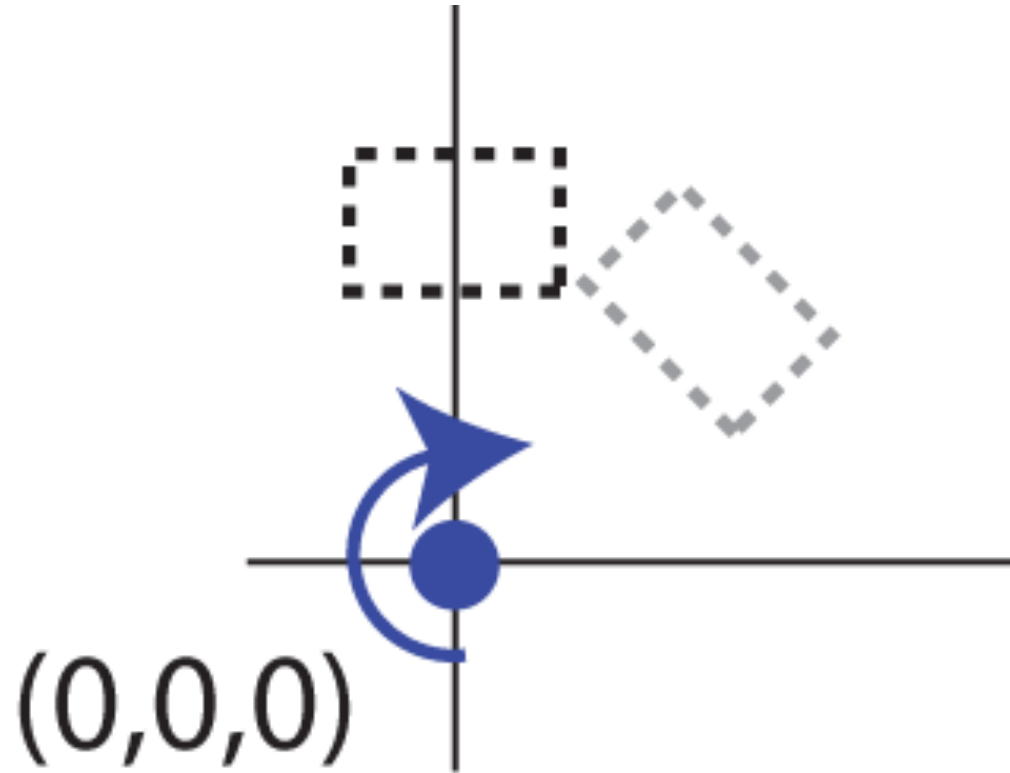
# Grid spacing

Commonly equal to full or half of the window size

For efficiency, grid spacing can be much larger. This is the case for today's demo.



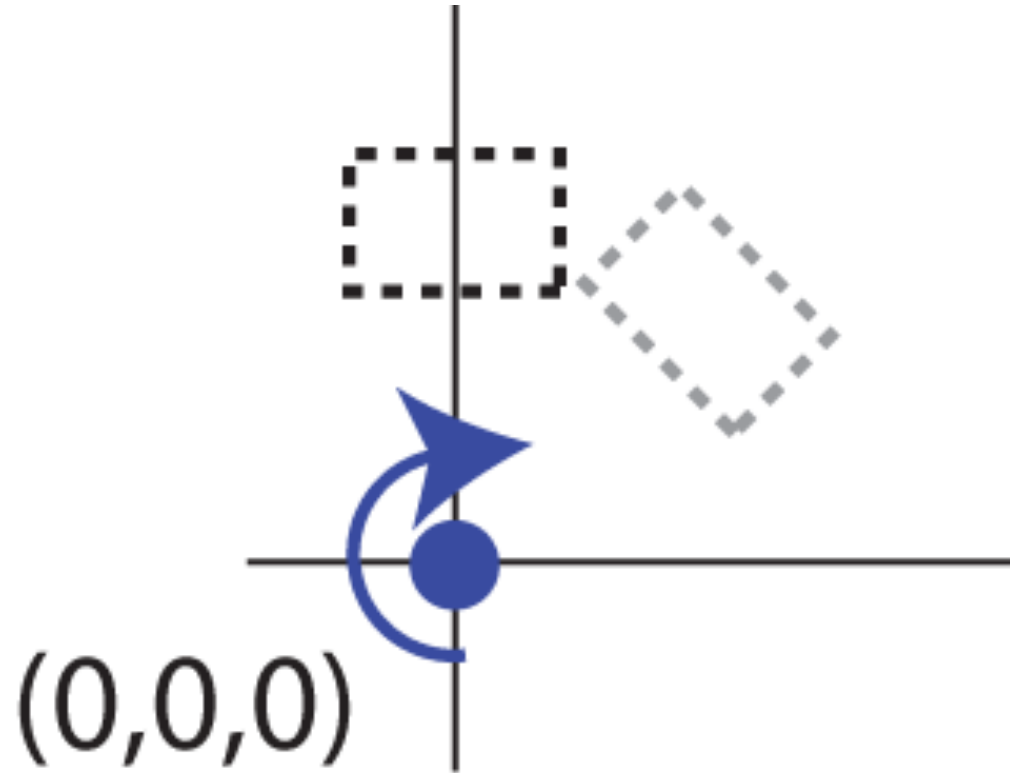
# Coordinate system origin



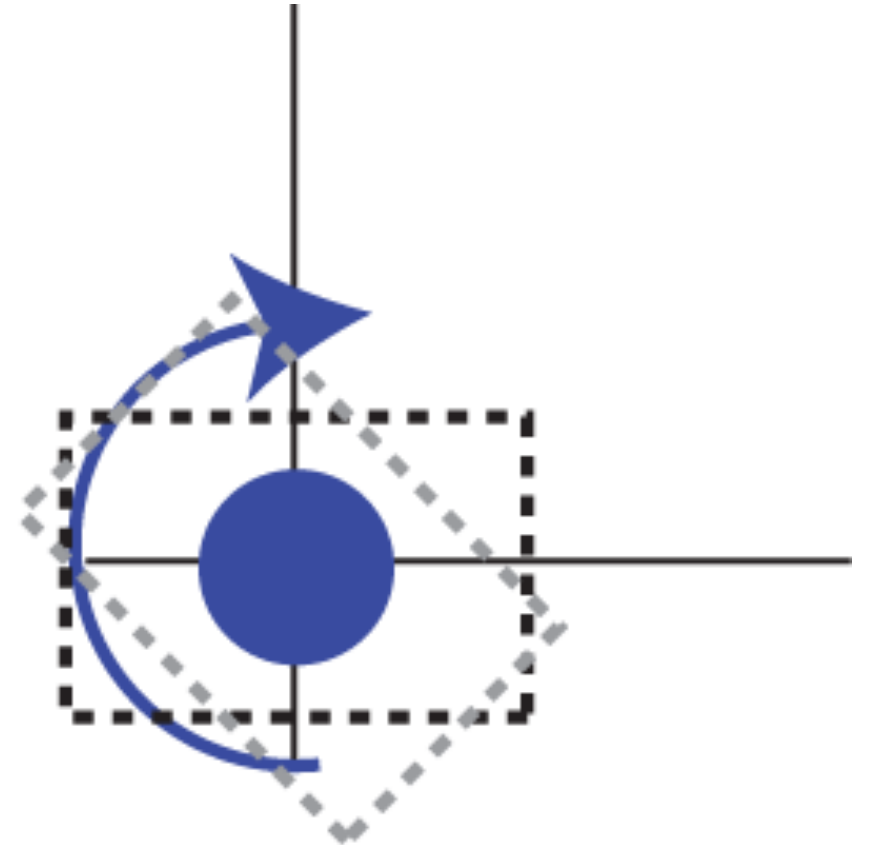
$(0,0,0)$

When the origin is offset from the point cloud window, the rotation and translation trade-off.

# Coordinate system origin

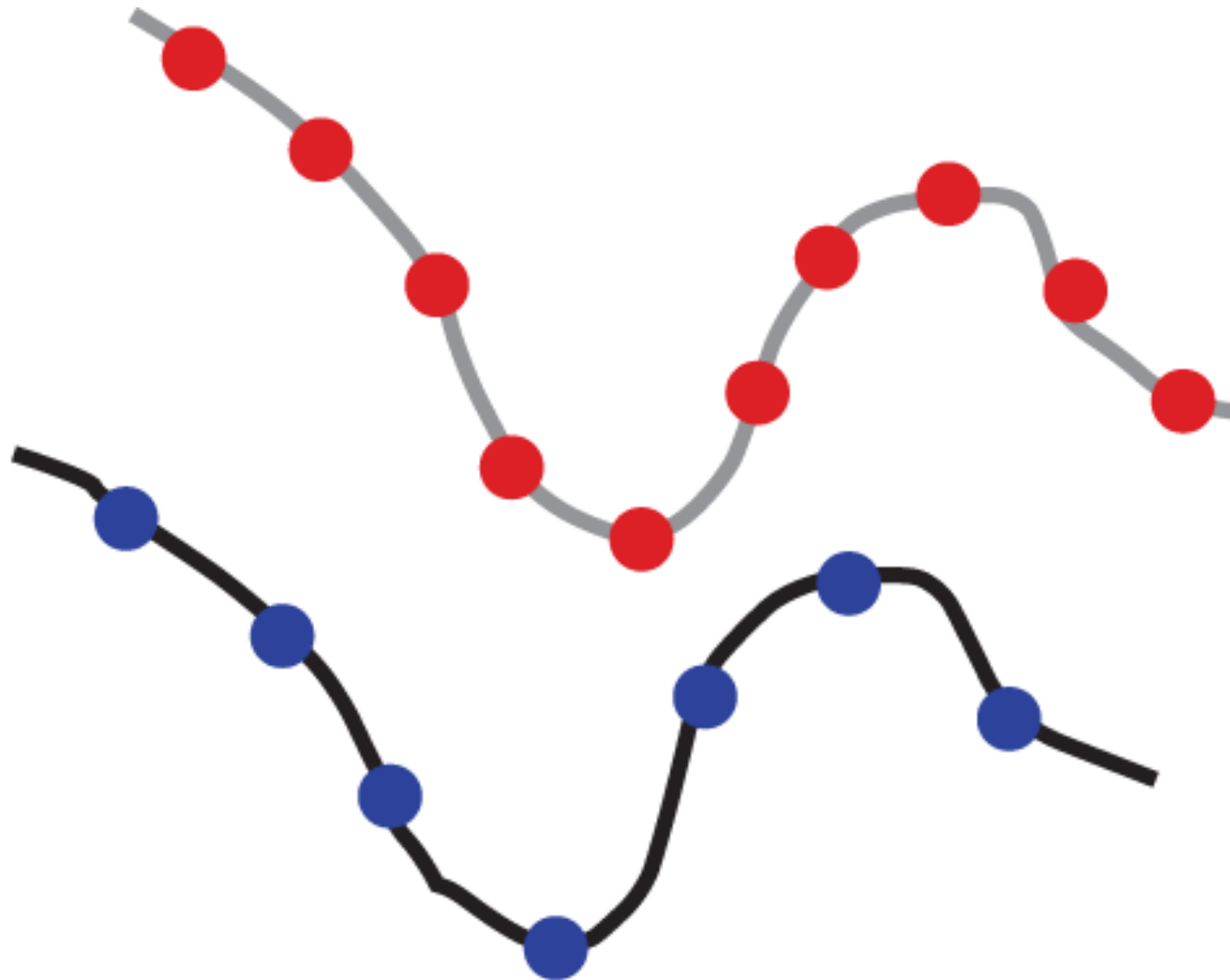


When the origin is offset from the point cloud window, the rotation and translation trade-off.



Shift the coordinate system origin  $(0,0,0)$  to the window center.

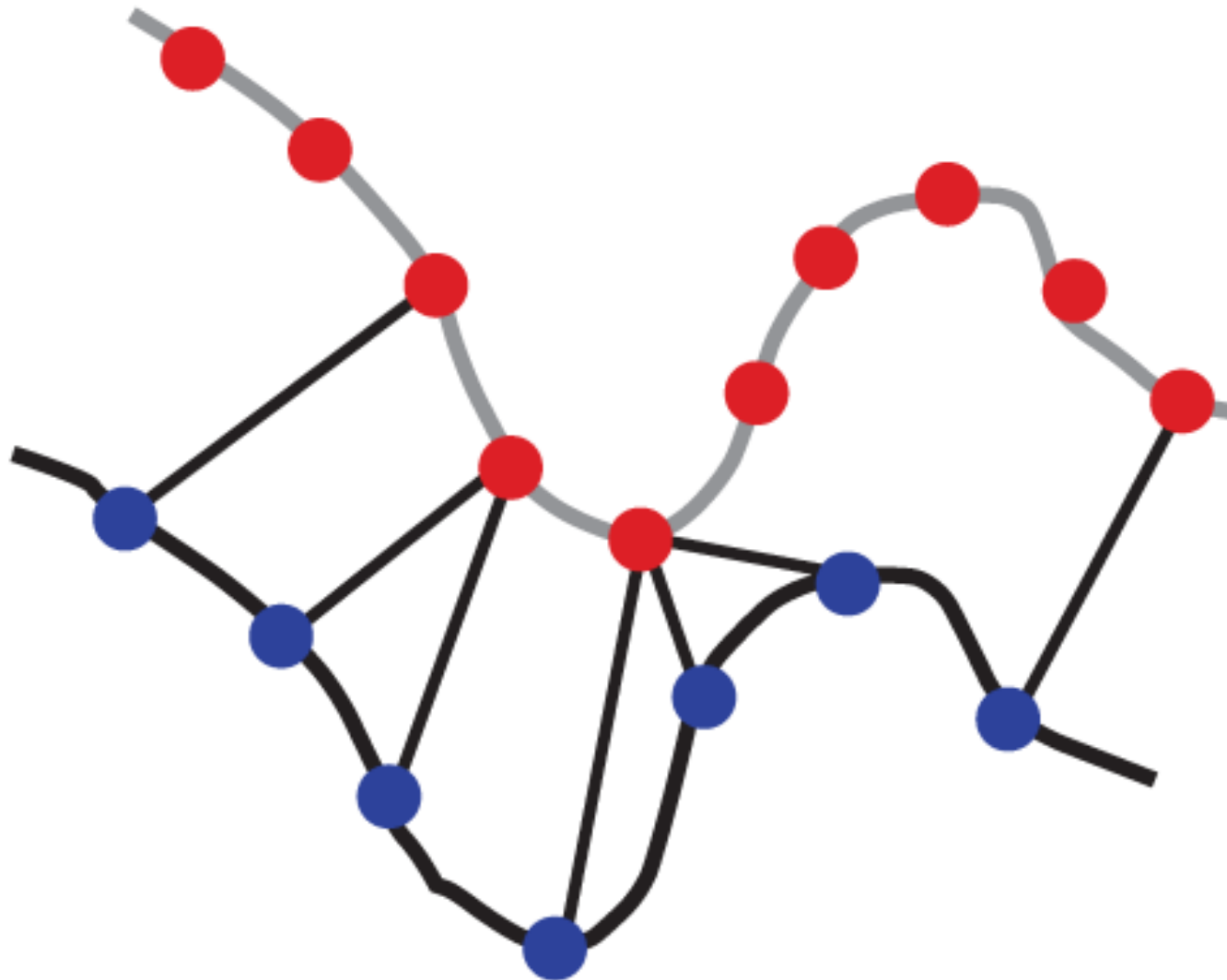
# Point Cloud Alignment and ICP Error



Pre-earthquake/  
Compare

Post-earthquake/  
Reference

# Point Cloud Alignment and ICP Error

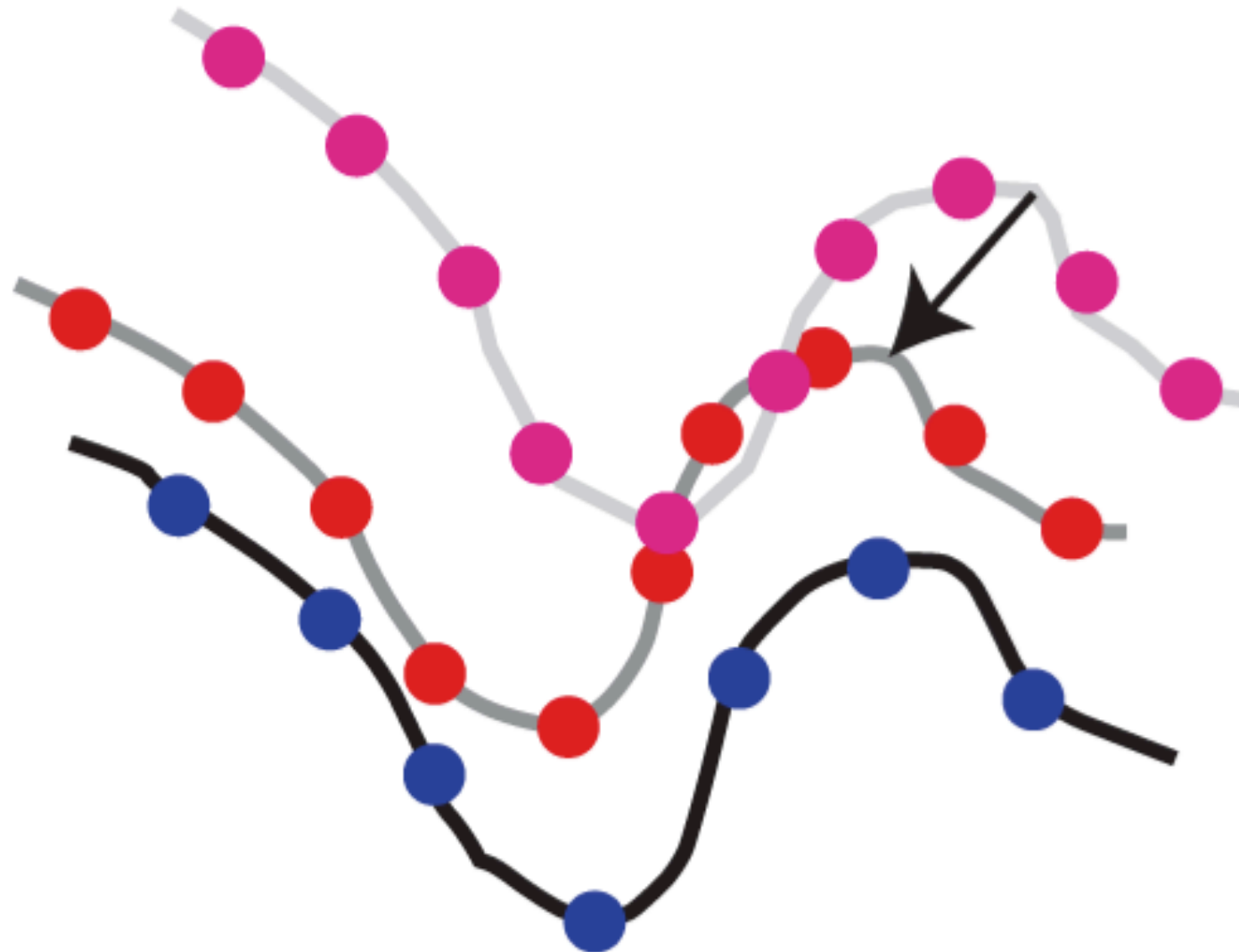


Pre-earthquake/  
Compare

Post-earthquake/  
Reference



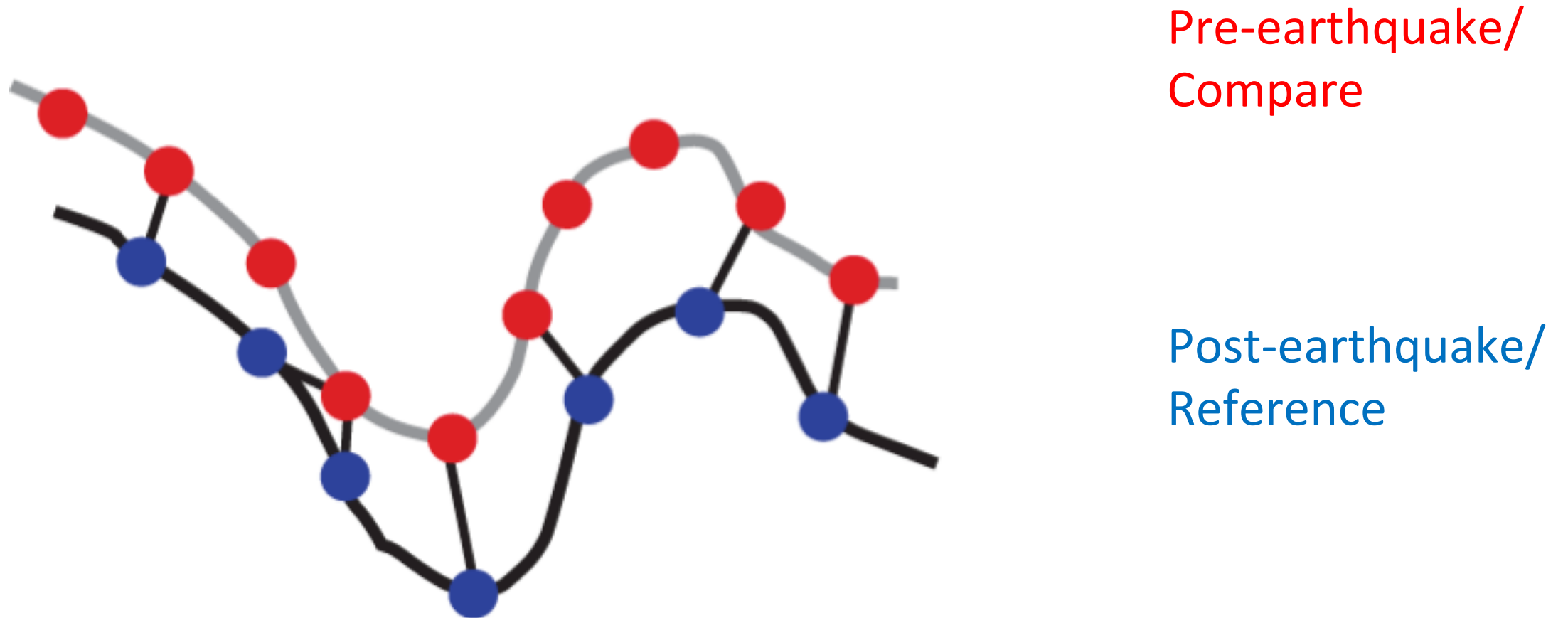
# Point Cloud Alignment and ICP Error



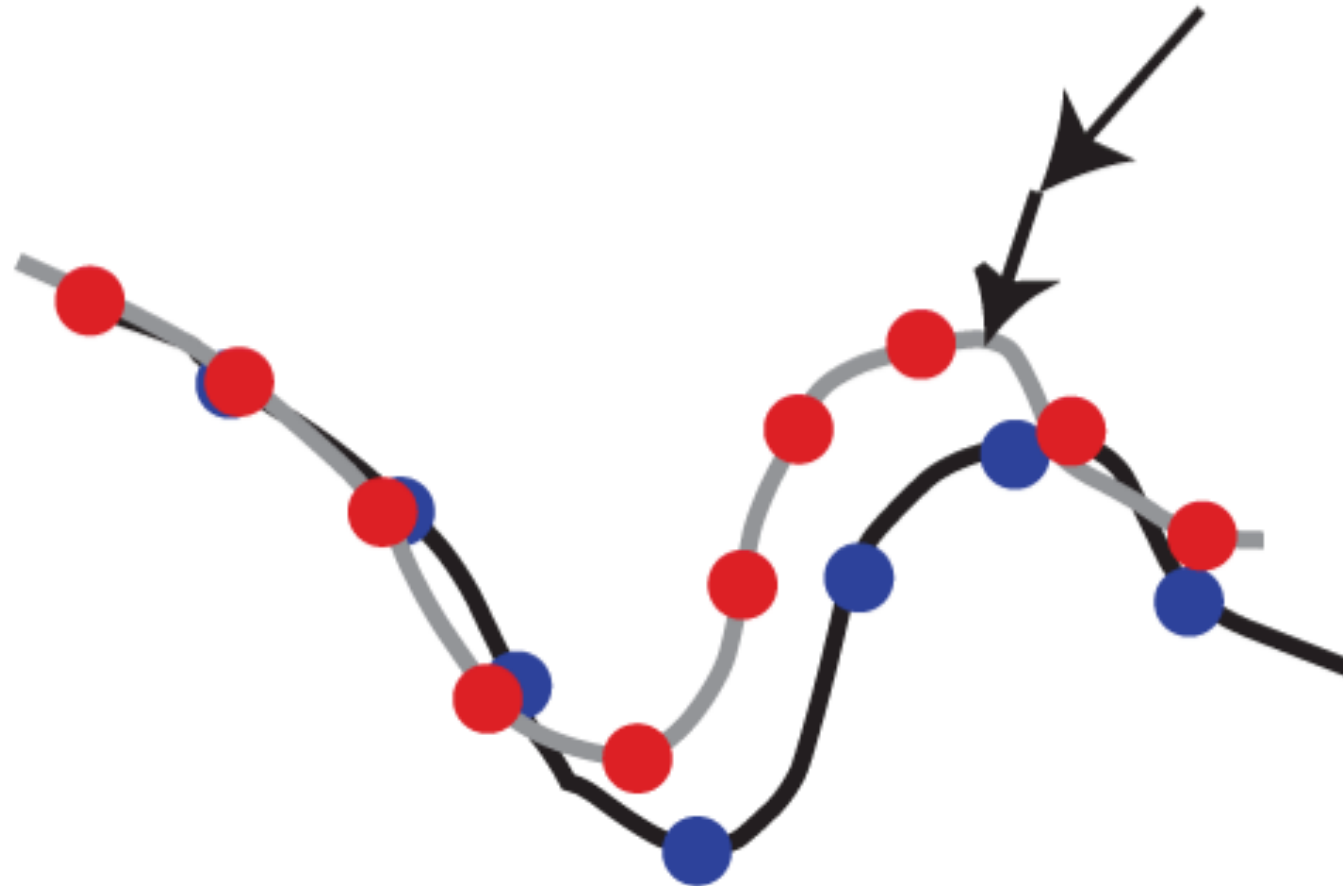
Pre-earthquake/  
Compare

Post-earthquake/  
Reference

# Point Cloud Alignment and ICP Error



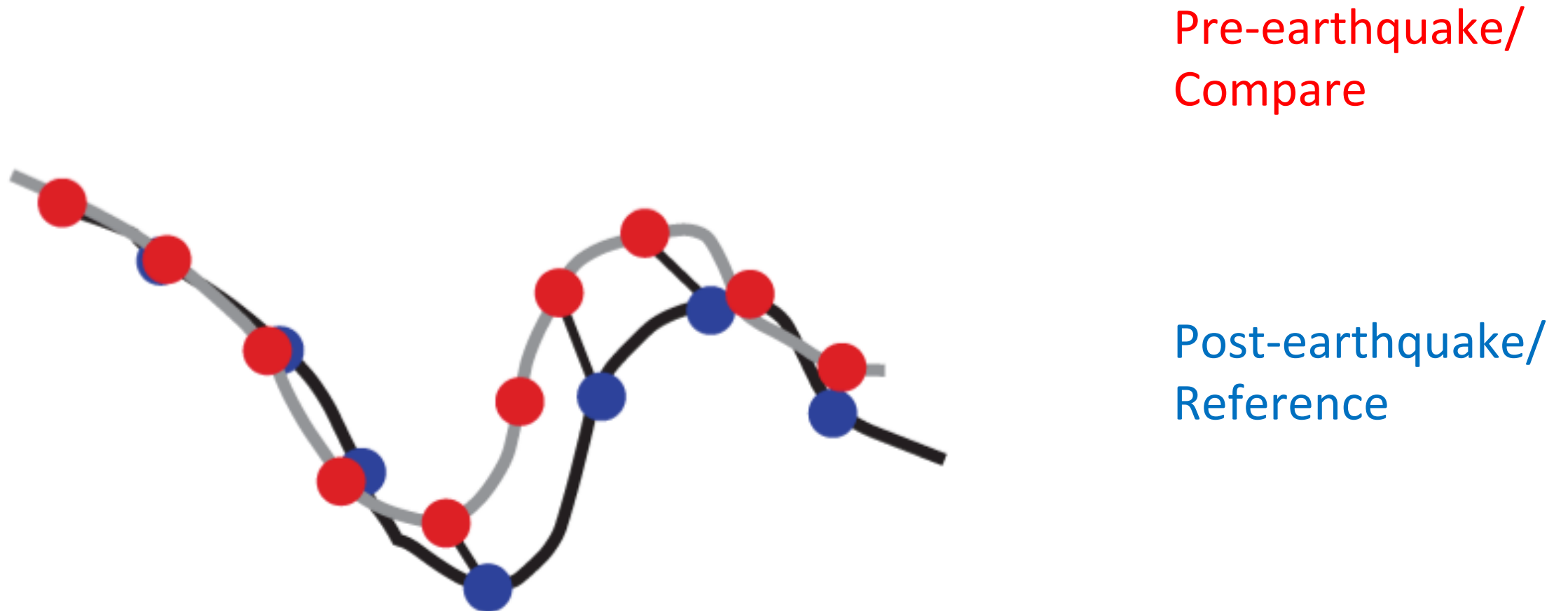
# Point Cloud Alignment and ICP Error



Pre-earthquake/  
Compare

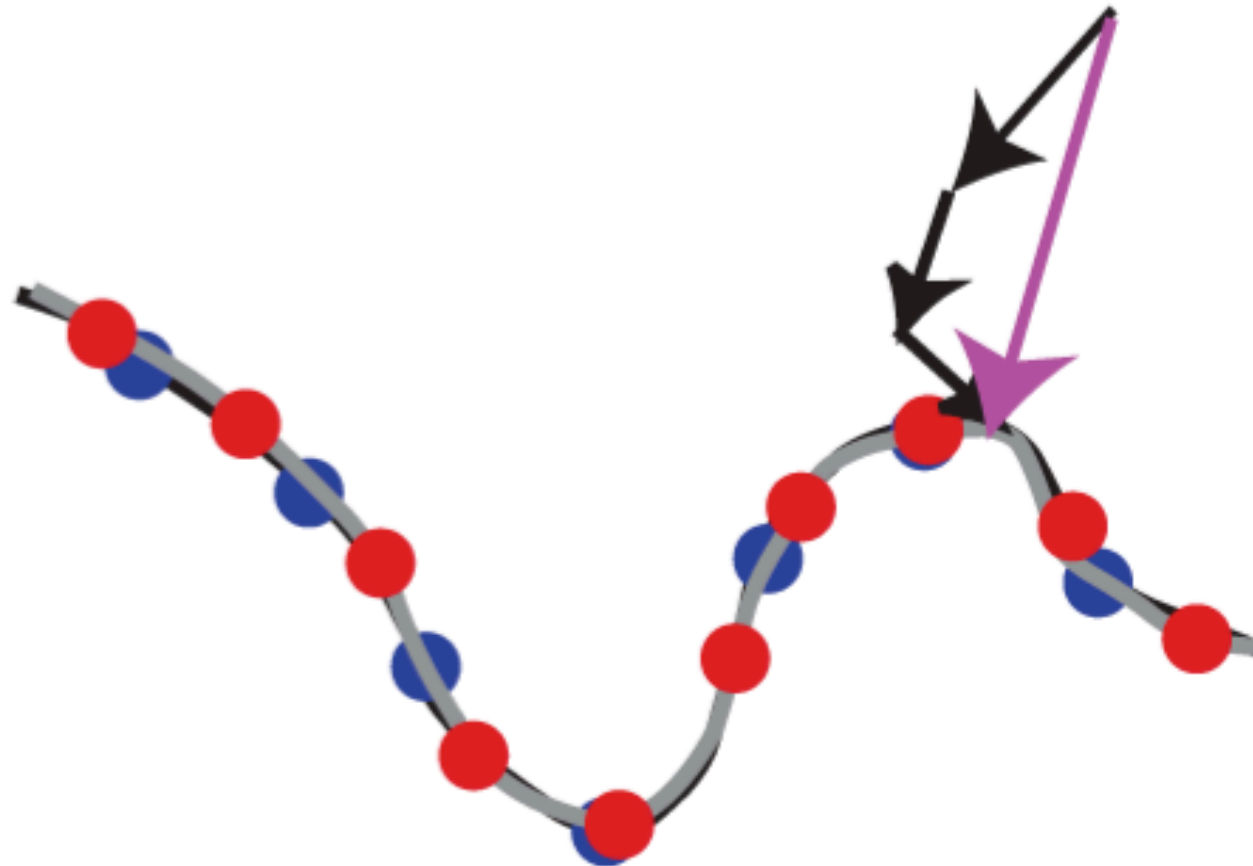
Post-earthquake/  
Reference

# Point Cloud Alignment and ICP Error



# Point Cloud Alignment and ICP Error

## Total deformation



Pre-earthquake/  
Compare

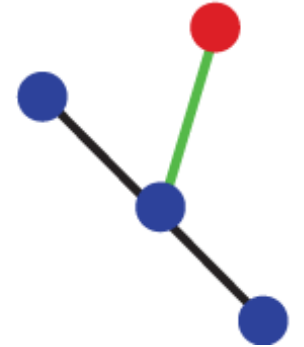
Post-earthquake/  
Reference

# Point cloud alignment error metrics

## Point-to-Point Error

*points in the REF cloud*  $\sum (\|\varphi(\text{COMPARE } i) - \text{REF } i\|)^2$

$\varphi$ : Rigid deformation

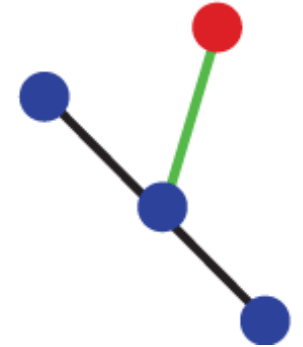


# Point cloud alignment error metrics

## Point-to-Point Error

$\frac{1}{N} \sum_{i=1}^N \|\varphi(\mathbf{p}_i) - \mathbf{r}_i\|^2$

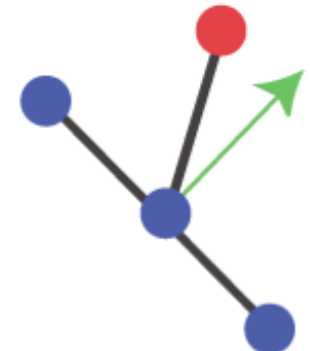
$\varphi$ : Rigid deformation



## Point-to-Plane Error

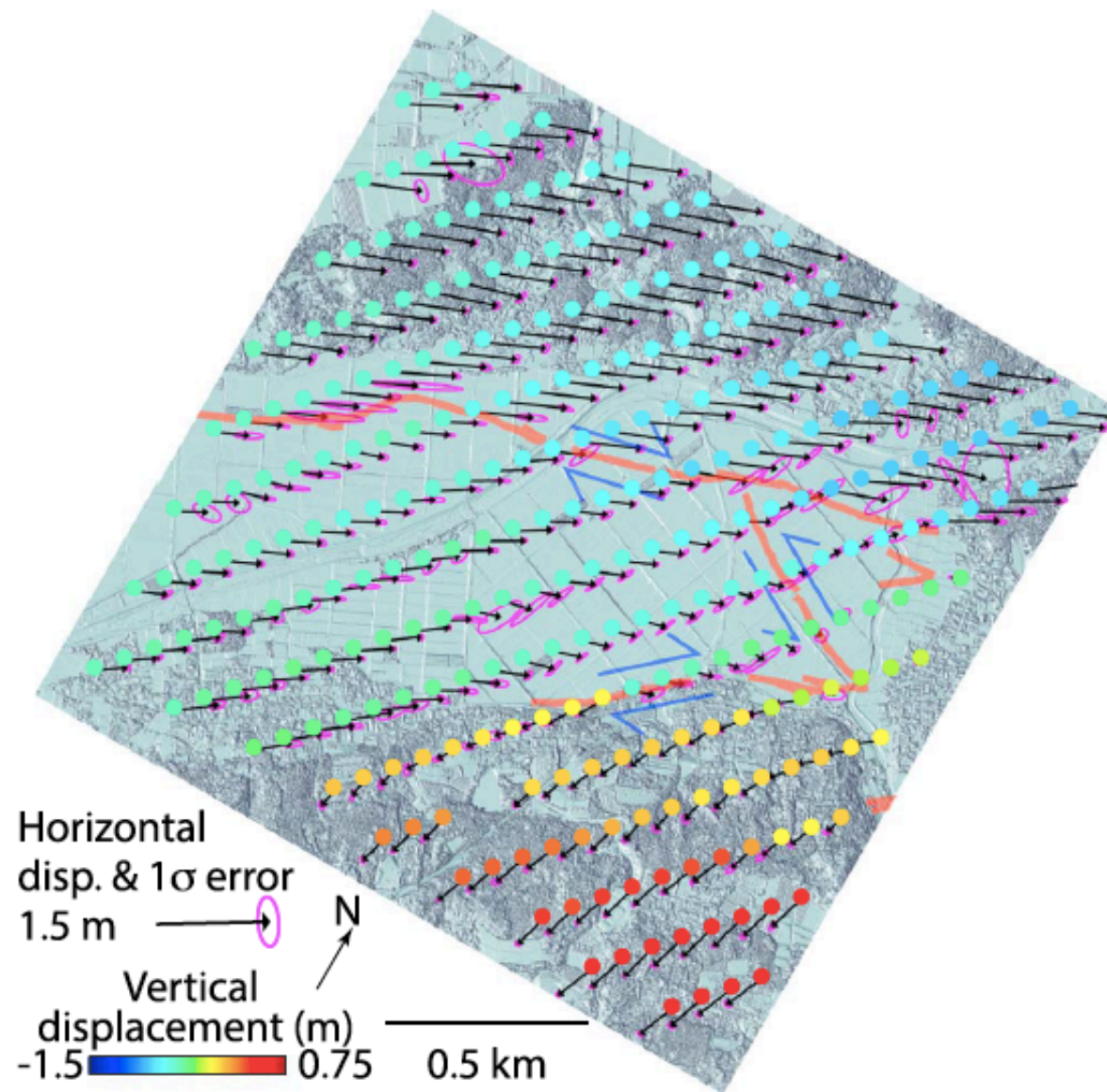
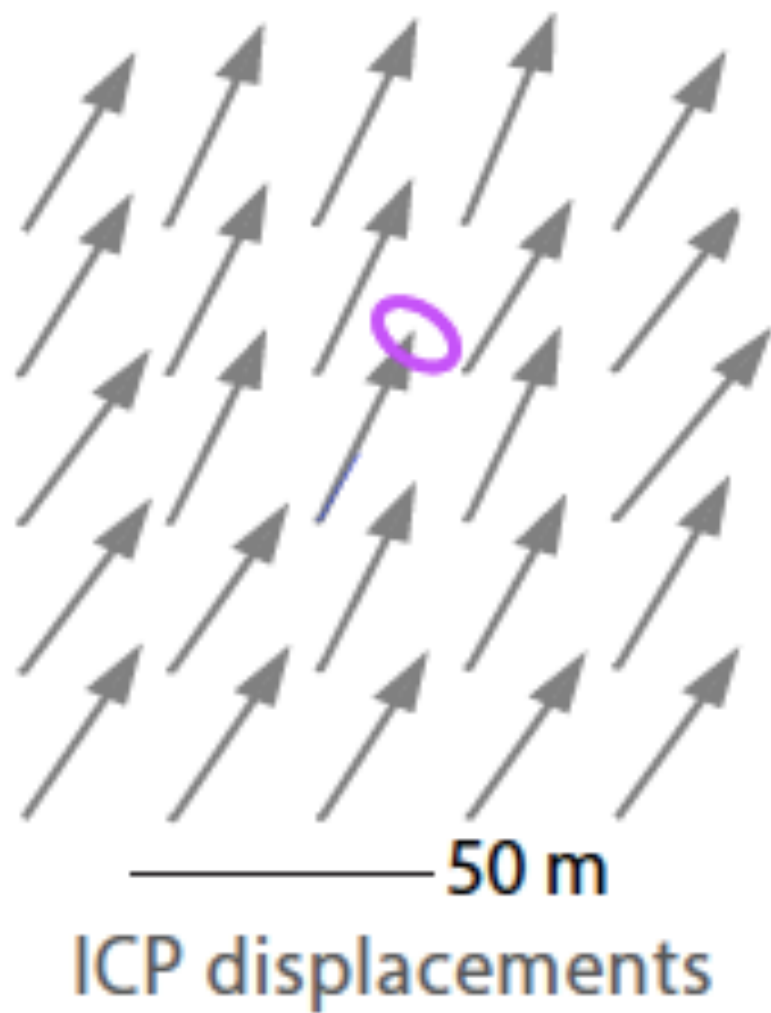
$\frac{1}{N} \sum_{i=1}^N \|\varphi(\mathbf{p}_i) - \mathbf{r}_i\| \cdot \|\mathbf{n}_i\|$

$\mathbf{n}_i$ : Vector normal to surface



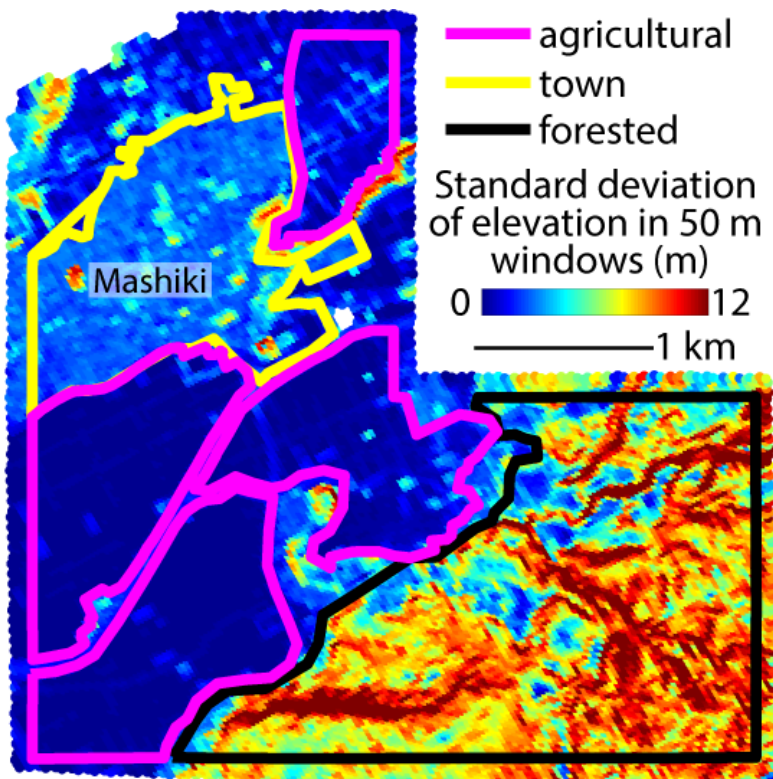
Point-to-plane works better for geological applications

# Correlation Error

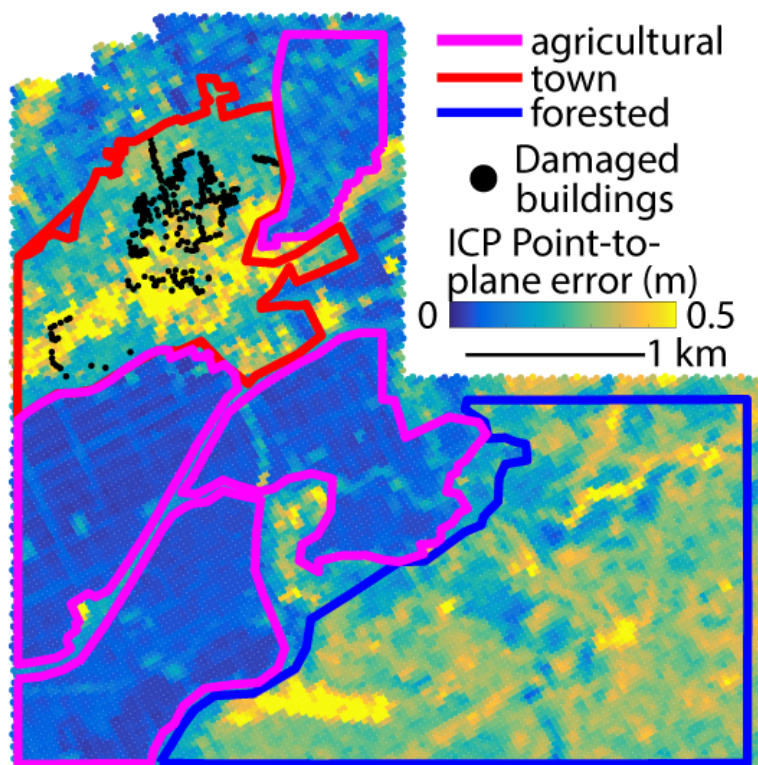




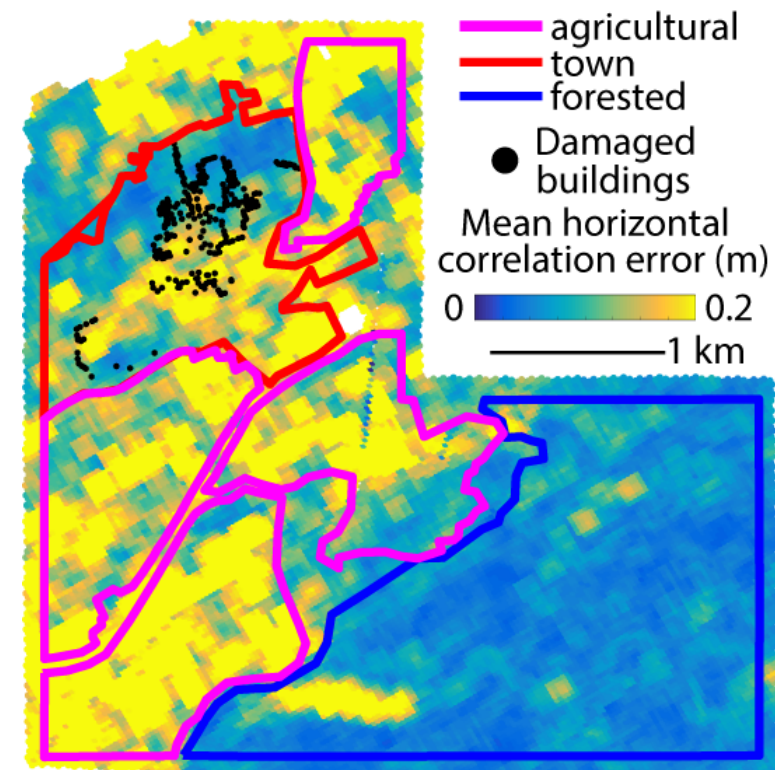
# Compare Different Error Measurements



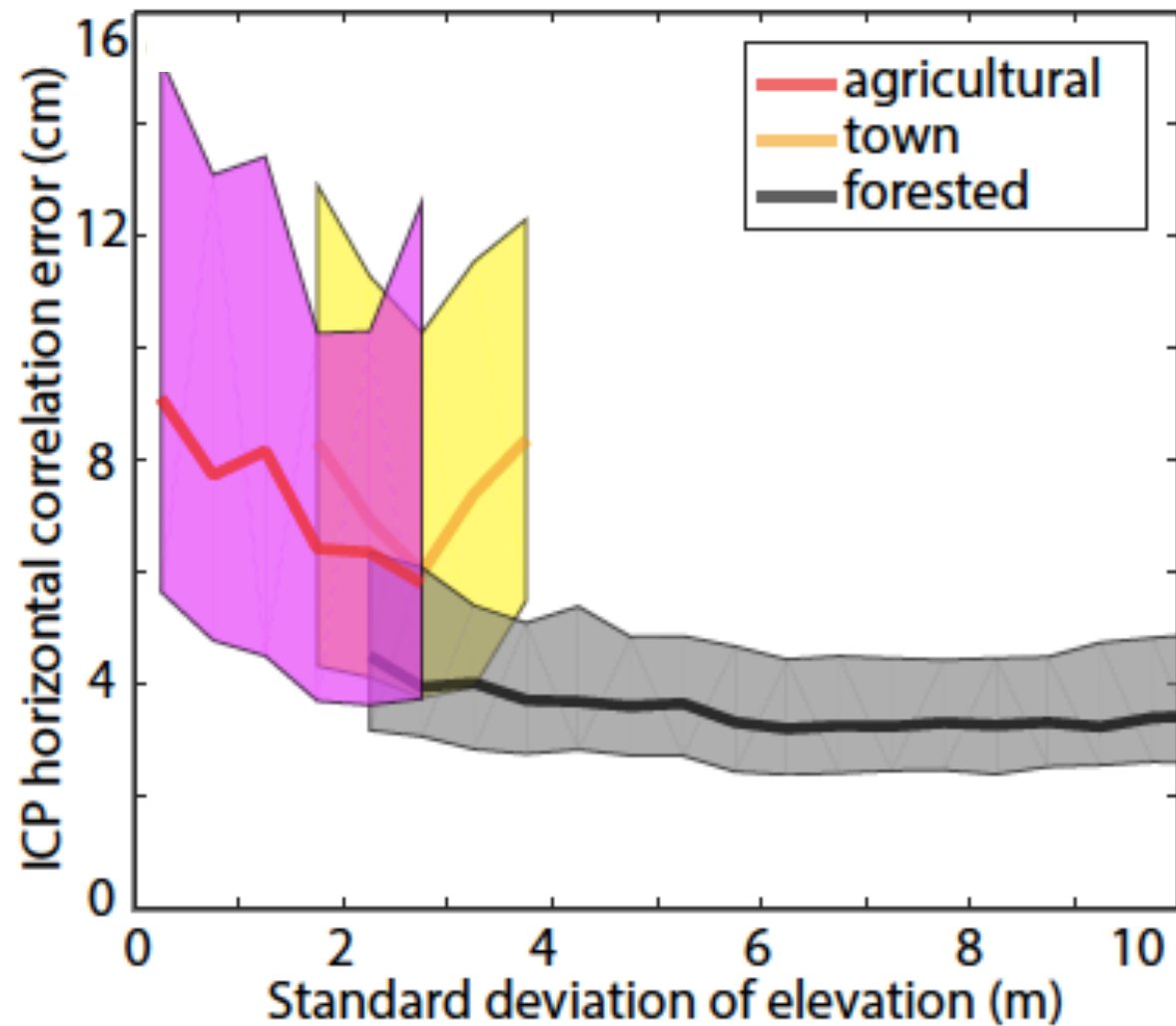
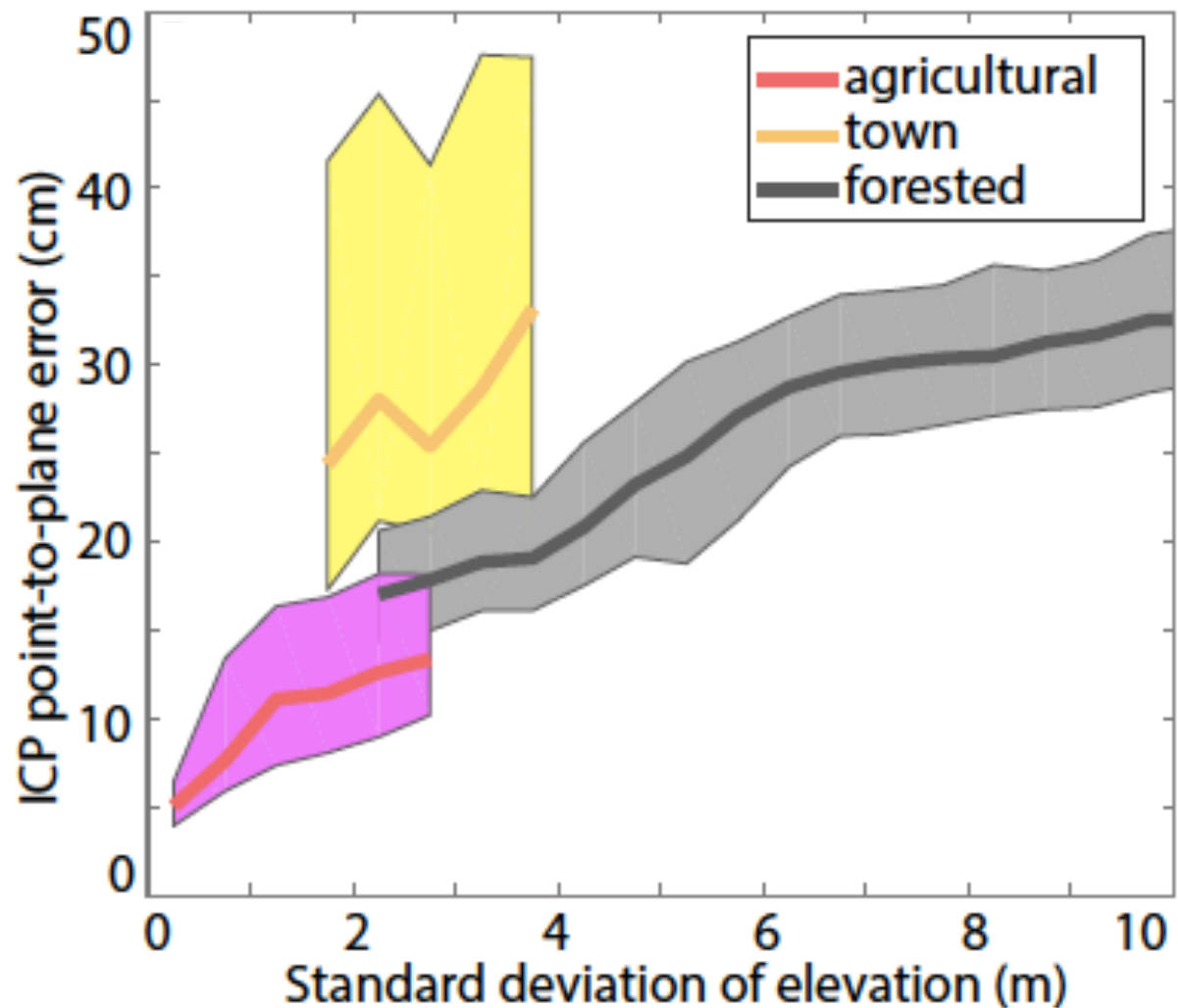
Standard deviation of Topography



ICP point-to-plane error



Horizontal correlation error



ICP point-to-plane error and ICP horizontal correlation error are anti-correlated.

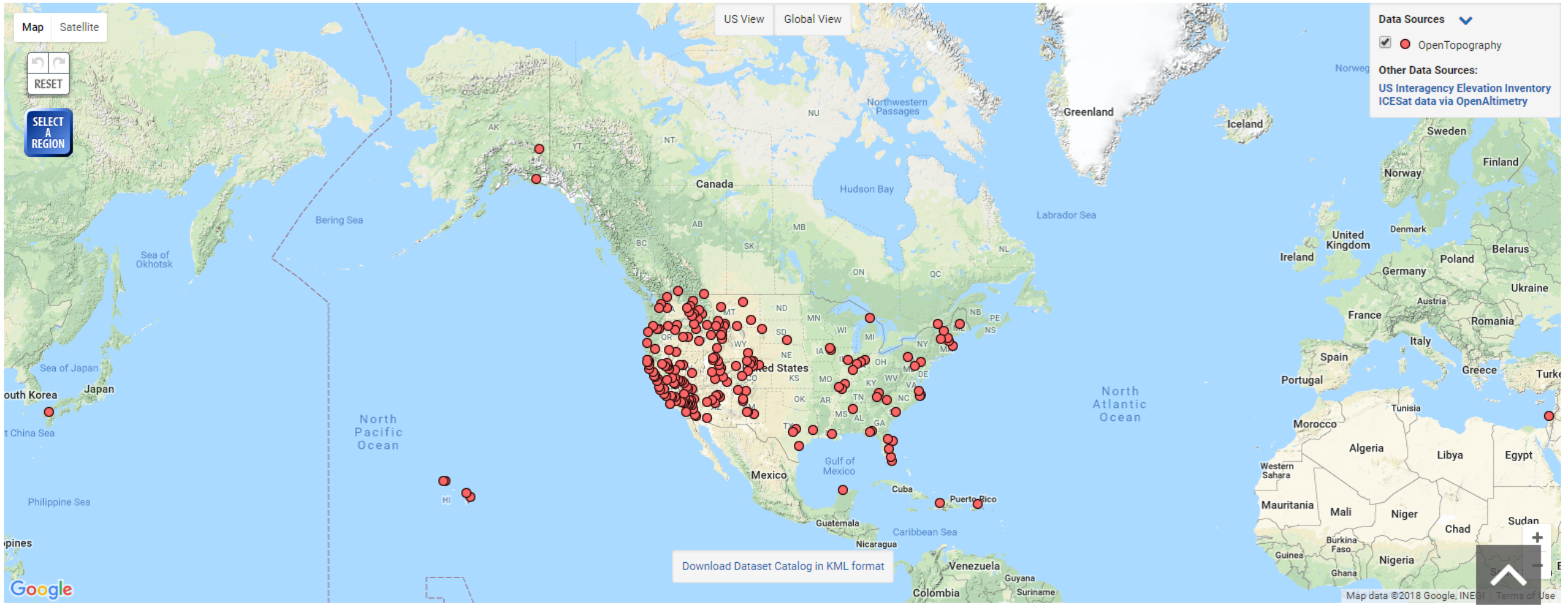
# ICP Differencing Demo

- Requirements

- Matlab
- ICP script for exercise
- Matlab ICP File Exchange (Jacob Wilm): <https://www.mathworks.com/matlabcentral/fileexchange/27804-iterative-closest-point>
- Matlab Las file reader ([Teemu Kumpumäki](#)): <https://www.mathworks.com/matlabcentral/fileexchange/48073-lasdata>

# Find Topography Data

Information and Instructions



Map Satellite

RESET

SELECT A REGION

US View Global View

Data Sources

- OpenTopography

Other Data Sources:

- US Interagency Elevation Inventory
- ICESat data via OpenAltimetry

Download Dataset Catalog in KML format

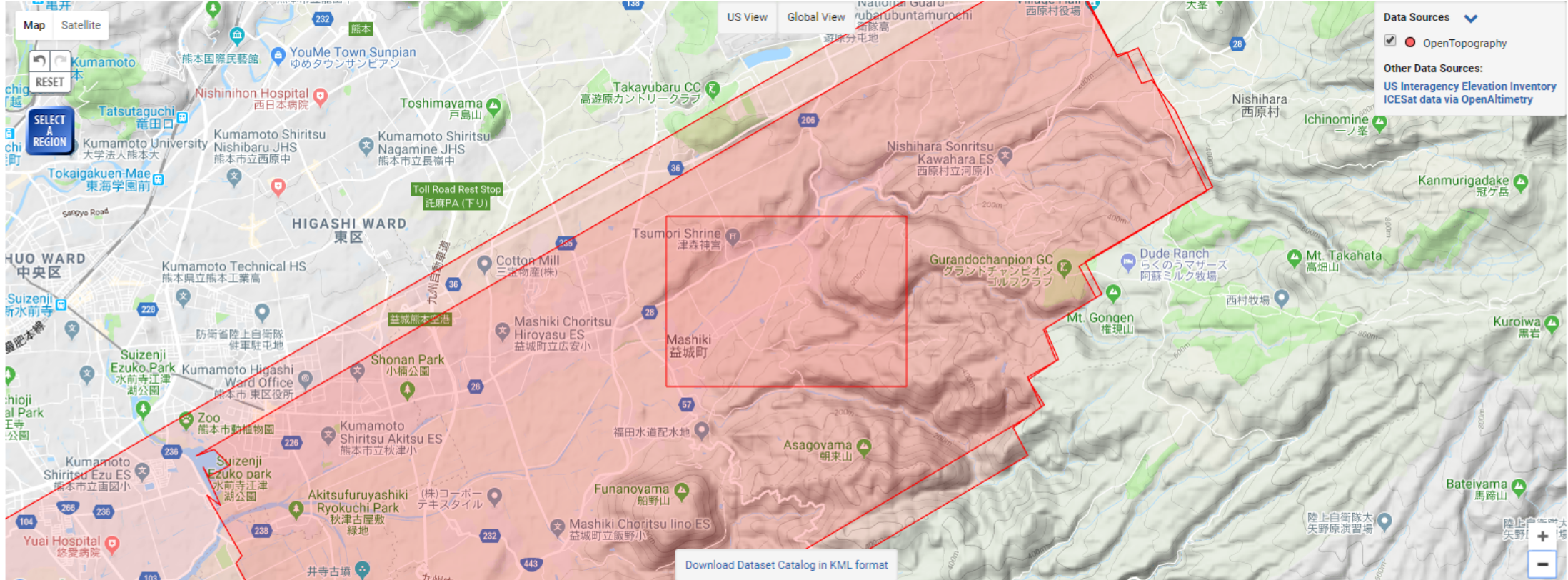
Map data ©2018 Google, INEGI Terms of Use

# Find Topography Data

Information and Instructions

The screenshot shows a Google Maps interface with the following elements:

- Map Style:** "Map" and "Satellite" buttons at the top left.
- Navigation:** "RESET" and "SELECT A REGION" buttons.
- Map View:** "US View" and "Global View" buttons.
- Data Sources:** A dropdown menu showing "OpenTopography" selected, with "Other Data Sources" including "US Interagency Elevation Inventory" and "ICESat data via OpenAltimetry".
- Map Content:** A topographic map of Japan with a red box highlighting the island of Kyushu. Labels for various regions and cities are visible, including Busan, Jeju, Kitakyushu, Fukuoka, Kumamoto, and Kagoshima.
- Download Button:** "Download Dataset Catalog in KML format" at the bottom center.
- Map Controls:** Zoom in (+) and zoom out (-) buttons at the bottom right.
- Map Data:** "Map data ©2018 Google, SK telecom, ZENRIN" at the bottom right.



**OpenTopography: 5 datasets found**



Datasets listed below are hosted by OpenTopography and are available in point cloud format for download and processing (e.g., creating custom DEMs). In some cases derived data products such as raster and Google Earth Image overlays are also available. Click the button to the right of the dataset name to access the available data products.

High Resolution Data		Global Data
1	Post-Kumamoto Earthquake (16 April 2016) Rupture Lidar Scan	<a href="#">Point Cloud Data</a>
2	Pre-Kumamoto Earthquake (16 April 2016) Rupture Lidar Scan	<a href="#">Point Cloud Data</a>

# Pre-Kumamoto Earthquake (16 April 2016) Rupture Lidar Scan

## Overview

The 16 April 2016 M7 Kumamoto earthquake ruptured the Futagawa- Hinagu fault zone on Kyushu Island of southwestern Japan. The lidar dataset collected by Air Survey Co., Ltd., of Japan covers the western half of the rupture zone. The acquisition of the imagery closely brackets the timing of the earthquake: The pre-earthquake dataset was acquired on 15 April 2016 and the post-earthquake dataset was acquired on 23 April 2016.



Platform: Airborne Lidar  
[Full Metadata](#)

Survey Area: 151.56 km<sup>2</sup>  
[Dataset Acknowledgement](#)

Point Density: 2.94 pts/m<sup>2</sup>  
Funder: AAS

Survey Date: 04/15/2016

Other Available Data Products: [Point Cloud Bulk Download](#)

## 1. Coordinates & Classification

Horizontal Coordinates: Japan Plane Rectangular Coordinate System (system 2) [EPSG: 2444]

Vertical Coordinates: JDG2000 [EPSG: 6694]

Data Selection Coordinates:  Manually enter selection coordinates (in the horizontal coordinate system listed above)

$X_{\min} = -15924.418161$     $Y_{\min} = -24166.962709$     $X_{\max} = -12080.574676$     $Y_{\max} = -21500.178931$

The selection area contains approximately 17,431,000 points.

Choose Return Classification  Ground  Unclassified  Vegetation

## 2. Point Cloud Data Download

Point cloud data in LAS format

Point cloud data in LAZ format

Point cloud data in ASCII format

## 3A. DEM Generation (Streaming TIN)

Gridding Method

Calculate TIN

Gridding Parameters

Grid Resolution (Default = 1 meter)

Max. triangle size (Default 50 units)

Grid Format

GeoTiff

Job Id	Dataset	Title	Submission	Completion	Duration	Num points	Final Status
pc1534078635822	JN16_KumapreEQ	pre_kumamoto_aug_2_1	2018-08-12 05:57:16	2018-08-12 05:58:37	81 secs	8,764,396	Done ✓

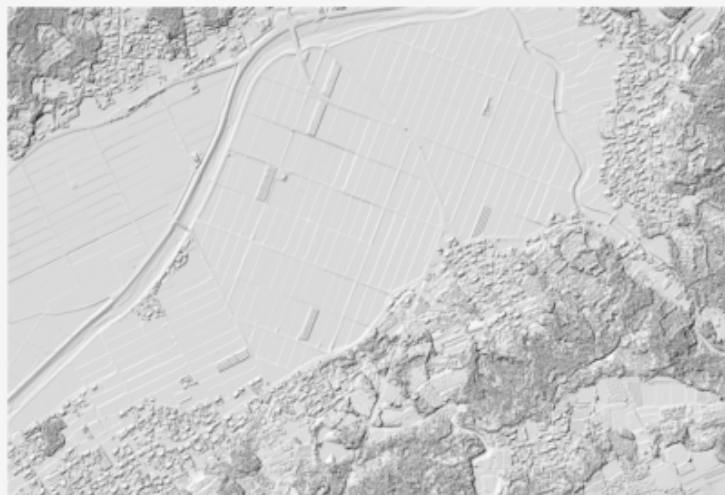
## Download Data

- Point Cloud Results
  - Download point cloud data in LAS format [points.las](#) (234 MB)
- DEM Results
  - Download DEM (TIN) [output.tin.tar.gz](#) (8.4 MB)
- Derivative Products
  - Download Hillshade & Slope Products (TIN) [viz.tar.gz](#) (11.1 MB)



## Visualization Products

- Ztin
  - [View with Google Map](#)



Repeat for the post-earthquake data



DEMO

# How do I perform topographic differencing on my own datasets?

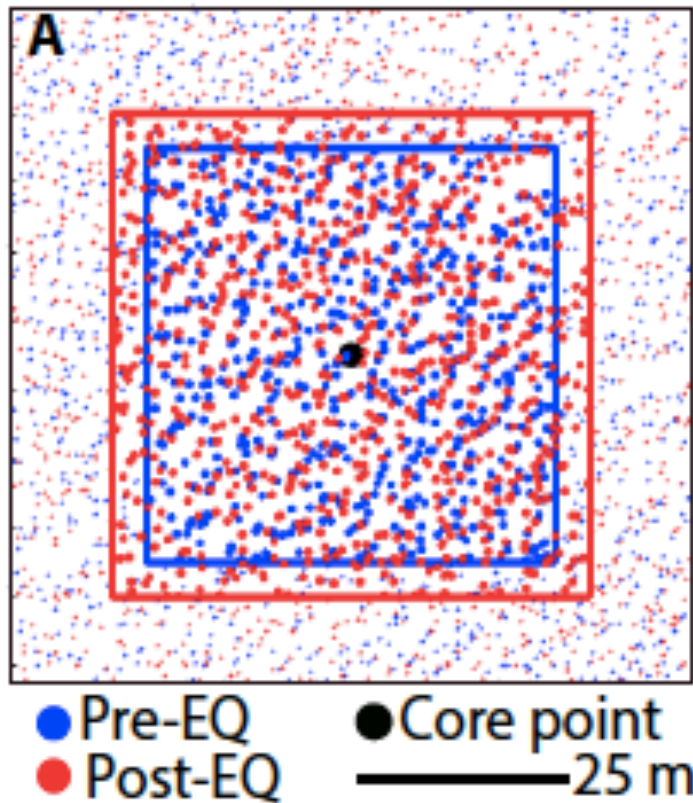
- Datasets
  - “Before” or “compare”
  - “After” or “reference”
- Datasets must be in the same reference frame
  - See lecture by Craig Glennie
- Datasets are big
  - Use lastile (lastools) to tile the big dataset into many smaller data files. Add a for loop to loop through the smaller data files.
- Datasets available on OpenTopography
  - 2010 El Mayor Cucapah earthquake
  - 2016 Kumamoto earthquake
  - ~12 OT datasets already in the same reference frame

# Software options

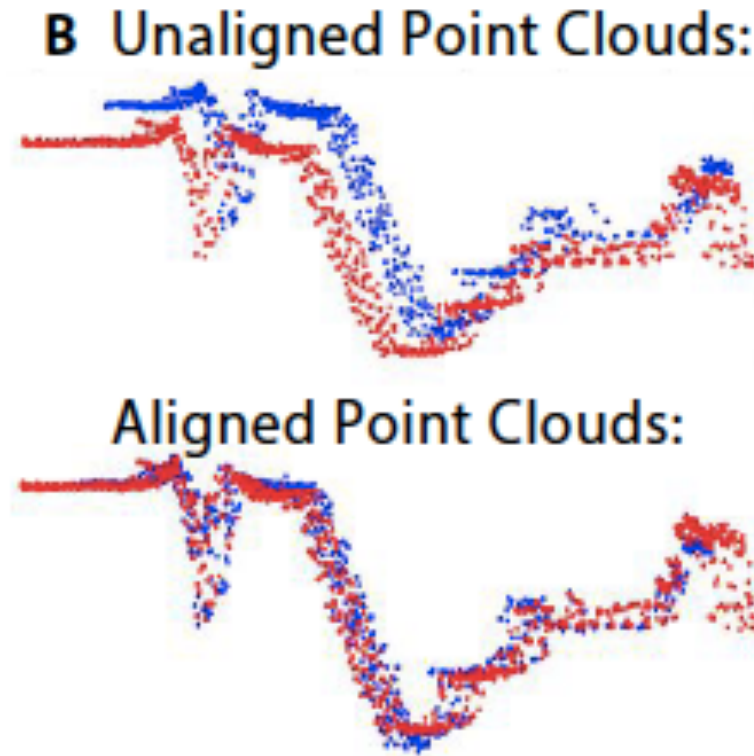
- Windowed ICP
  - LIBICP (<http://www.cvlibs.net/software/libicp/>): C++ code with Matlab wrappers
  - Matlab ICP File Exchange (Jacob Wilm): <https://www.mathworks.com/matlabcentral/fileexchange/27804-iterative-closest-point>
  - PDAL: <https://pdal.io> (Point Data Abstraction Library)
- Global ICP
  - Point Cloud Tools File Exchange: <https://www.mathworks.com/matlabcentral/fileexchange/54412-point-cloud-tools-for-matlab>
  - 2018 Matlab built in functions: <https://www.mathworks.com/help/vision/ref/pcregrigid.html>

Thank you!

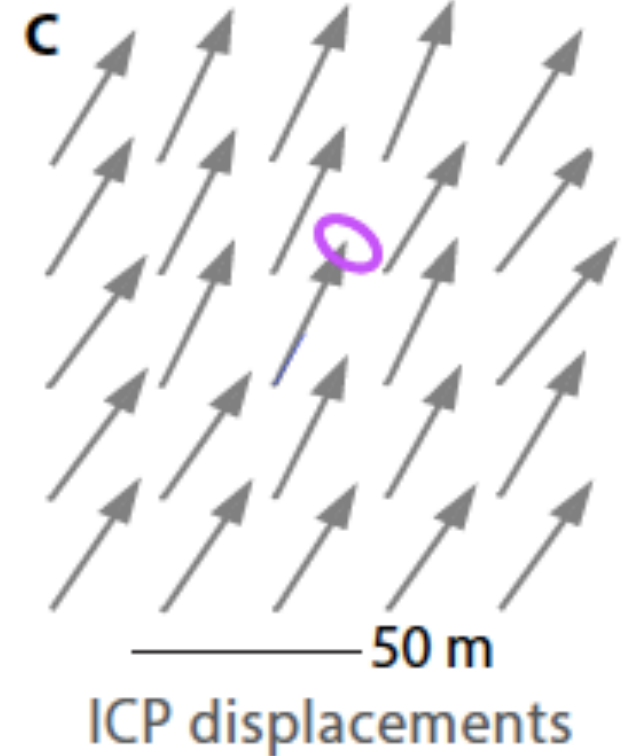
# 3D coseismic displacement: Iterative closest point (ICP)



Windowed subset



3D rigid-body  
deformation



Uncertainty