## *Topographic metrics and bedrock channels* Outline of this lecture

- Topographic metrics
- Fluvial scaling and slope-area relationships
- Channel steepness sensitivity to rock uplift





# **Topographic Metrics**

- Many Topographic metrics have been proposed. We'll examine the three most common
  - Channel Steepness Index
  - Hillslope Gradients
  - Local Relief at Various Scales
  - Chi (Bodo lecture)
- What are the relationships among these?
- Which are most useful for gaging the influence of tectonics on topography?









## 80-90% Relief is on Bedrock Channels



#### Blue lines: drainage area > 1km<sup>2</sup>



Advancing understanding of geomorphology with topographic analysis emphasizing high resolution topography June 12-15, 2017





# Fluvial Scaling – Empirical Data

• Empirical data for well-adjusted fluvial systems around the globe yield the following scaling:

$$S = k_s A^{-\theta}$$



- Linear relationship between log(S) and log(A)
- $k_s$  is the channel steepness;  $\theta$  is the concavity

### Flint's Law: Mixed Bedrock-Alluvial Stream (Appalachians, VA)



drainage area (m<sup>2</sup>)

## Flint's Law: Mixed Bedrock-Alluvial Stream (Appalachians, VA)



drainage area (m<sup>2</sup>)

k<sub>s</sub> is a general morphometric index: No dependence on basin shape

### Duvall, Kirby, and Burbank, 2004, JGR-ES

U = Rock Uplift Rate

# Concavity (θ) invariant with U

#### Steepness (Ks) varies with U



# Siwalik Hills, Nepal





VIE-L

### Active folding of fluvial terraces across the Siwaliks Hills, Himalayas of central Nepal

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JOURNAL OF GEOPHYSICAL RESEARCH, VOL. 105, NO. B3, PAGES 5735–5770, MARCH 10, 2000 --K. X Whipple

## **Bagmati Transect**



#### Data from Lave and Avouac, 2000, JGR

#### --K. X Whipple

# Bakeya Transect



# Siwalik Hills Anticline Himalaya Foreland, Nepal



# Strike-Parallel: Normal, uniform concavity



Strike-Parallel: Steepness varies with U

# Siwalik Hills, Nepal



#### Tectonic Geomorphology of the San Gabriel Mountains http://qfaults.cr.usgs.gov

http://earthquake.usgs.gov/anss/



# Shaded Relief with Color = Elevation



srtm\_bigtujunga30m\_utm11.tif



## Distance from divide

Beware: Many authors use "hillslope relief" and "local relief" (measured over up to 5km radius) as interchangeable --K. X Whipple Streams by Normalized Steepness Index

Local Relief (r = 2.5km)



*Note:* abrupt steepness breaks across active faults, no break where inactive/slow --K. X Whipple

#### Geological Society of America Special Paper 398 2006

#### Tectonics from topography: Procedures, promise, and pitfalls

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#### ABSTRACT

Empirical observations from fluvial systems across the globe reveal a consistent power-law scaling between channel slope and contributing drainage area. Theoretical arguments for both detachment- and transport-limited erosion regimes suggest that rock uplift rate should exert first-order control on this scaling. Here we describe in detail a method for exploiting this relationship, in which topographic indices of longitudinal profile shape and character are derived from digital topographic data. The stream profile data can then be used to delineate breaks in scaling that may be associated with tectonic boundaries. The description of the method is followed by three case studies from varied tectonic settings. The case studies illustrate the power of stream profile analysis in delineating spatial patterns of, and in some cases, temporal changes in, rock uplift rate. Owing to an incomplete understanding of river response to rock uplift, the method remains primarily a qualitative tool for neotectonic investigations; we conclude with a discussion of research needs that must be met before we can extract quantitative information about tectonics directly from topography.



- Matlab Codes are unchanged from previous version
- A few improvements (tutorial is still for the 9.X version):
  - Append files on import works better you don't get multiple copies of the merged shapefile loading up in arcmap
  - Hot links to pop up the matlab output figures now work on the merged shapefile, so you can click any channel with the lightning strike and view the channel profile and fits you may have done.
  - A few error catches have been added to warn users if



Contents lists available at SciVerse ScienceDirect

### Journal of Structural Geology

journal homepage: www.elsevier.com/locate/jsg

Review

### Expression of active tectonics in erosional landscapes

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STRUCTURAL

# Channel steepness considerations

"By evaluating slope-area regressions using a reference concavity index ( $\theta_{ref}$ ), one can determine a normalized steepness index ( $k_{sn}$ ) that allows effective comparison of profiles of streams with greatly varying drainage area" (Wobus, et al., 2006)

$$S = k_{sn} A^{-\theta_{ref}}$$

Stream-power family of incision models

 $E = KA^m S^n$ 

(*E* is erosion rate, *K* is a generalized rate constant, *A* is drainage area, and *S* is local slope)









# Channel steepness considerations

At steady state, by definition the channel erosion rate is equal to the uplift rate of rock (E = U), and the steady-state channel gradient( $S_e$ ) is Recall:

$$S_e = (U/K)^{1/n} A^{-m/n} \qquad S = k_{sn} A^{-\theta_{ref}}$$

predicts  $\theta \sim \frac{1}{2}$ , consistent with observations for well-graded channels with uniform *K* and *U* (0.4 <  $\theta$  < 0.6)

And thus we assume,  $K_{sn} \sim U^p$  (rock uplift rate) all other things (like climate, vegetation, and rock resistance to erosion, [that is K], being roughly equal)













# Transient channel response and knickpoints downstream region adjusting to response and knickpoints

Migrating boundaries between downstream region adjusting to new forcing (e.g., baselevel drop) and upstream region adjusted to prior state



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## Interpretation of transient profiles



distance from outlet (km)

Kirby and Whipple, 2012



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